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Students' Problem-solving Difficulties and Coping Strategies in Mathematics: A Model- Building Study

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Abstract. A number of research projects in educational assessment reveal that students struggle when it comes to accomplishing problem-solving tasks in Mathematics. Such a struggle is primarily due to the complexities of problem-solving. Students deal with these struggles by employing mechanisms that could be classified into either problem-focused or emotion-focused coping strategies. The study was implemented through a design-research approach by using a model-building framework with four stages: 1) analysis; 2) development; 3) implementation/validation; and 4) evaluation. The models with the two variables were also linked to the student's sexual orientation and academic programs. Through descriptive statistical measures, such as frequency count and percentages, difficulties were enumerated through the administration of a problem-solving test. It should be noted, however, that a respondent may have at least one difficulty in the different phases of problem-solving. Two hundred and ninety-seven of the 425 college respondents were involved in the model-development stage. The majority of both males and females experienced the same difficulty/ies in all the phases, namely; the inability to distinguish the known from the unknown information (U1), the inability to transform a problem into a mathematical equation (D1), the inability to completely perform the working procedure systematically and accurately (C1), and the inability to start the evaluation of the correctness of the obtained solution (L2). The majority of the respondents of both the STEM-related and non-STEM-related academic programs experienced the same difficulties, namely: D1, C1 and L2 in the DP, CP and the LB problem-solving phases, respectively. In the UP phase,

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however, the majority of the respondents in the STEM-related academic programs experienced U2, and U1 for the non-STEM-related academic programs. Moreover, 43 acts of coping were elicited from the respondents through a coping-strategy questionnaire, 32 of which were classified as problem-focused, whereas 11 were categorized as emotion-focused. Both sexes utilized the coping strategies: UP2, DP8 and CP7 in the phases of UP, DP and CP respectively. In the LB phase, LB3 was utilized by the males and LB1 was utilized by the females. The majority of the respondents of the STEM-related academic programs preferred UP2, DP8, CP7 and LB1 coping strategies, while UP2, DP8, CP7 and LB3 opted for the non-STEM related academic program respondents. The identified relationships between and among the variables brought forth two models namely: Coping Strategy by Sex by Phase, and Coping Strategy by Academic Program by Phase. Purposive sampling factors, like the availability of the respondents and the matching of coping strategies, as presented in the models developed were taken into consideration in evaluating the effectivity of the models. From the sampled respondents in the validation group, where the frequency of their pre-identified difficulties had either decreased or were totally resolved. The study concludes that the models have the ability to address the difficulties of the students in their problem-solving encounters through their coping strategies. Therefore, this study recommends that teachers should provide students with problem-solving tasks that focus on the phases in which they struggle. Additionally, this study encourages teachers to allow their students to apply their most-preferred coping strategies, so that they could perform better in Mathematics problem-solving.

Keywords: Mathematics problem-solving; problem-solving difficulties; problem-solving coping strategies; model-building

1. Introduction

Studies on educational assessment show that students experience difficulties in Mathematics, particularly in problem-solving. This could be a difficulty in at least one of the four phases (Polya, 1945), namely: understanding the problem, devising a plan, carrying out the plan, and looking back. Moreover, other studies also examined the diverse ways in which students cope with such difficulties. These coping strategies are commonly classified under two general categories, which are problem-focused and emotion-focused (Folkman & Lazarus, 1980; 1985). Nevertheless, studies that investigate how these variables are associated with learners' sexual orientations and/or academic programs are scarce.

A number of studies related to problem-solving difficulties abound in the online literature. In the scholarly work of Siniguan (2017), respondents demonstrated difficulties in carrying out the plan and looking-back phases. Sultan's (2014) study, on the other hand, revealed that students have difficulty in translating word problems into mathematical phrases, when given word problems in Algebra. In a similar vein, the study conducted by Dela Cruz and Lapinid (2014) also found that learners not only struggle in translating word problems, but also experience difficulty in Mathematics, due to carelessness, lack of comprehension, interchanging values, and unfamiliar words. Meanwhile, Ferguson (1980)

believed that students have “reading” deficiencies, where symbols and abstractions are concerned. This deficiency can be classified under Polya’s (1945) understanding of the problem phase.

According to Ferguson (1980), reading does not simply refer to the ability to pronounce the words, or attach names to the symbols, rather, it necessitates the ability to comprehend the material. Studies embarking on different academic programs correspondingly reveal the problem-solving difficulties of students. In a science class, Nikmah et al. (2019) found that students struggle in devising a plan, when they tried to get the maximum value through the concept of first derivatives of algebraic functions. Meanwhile, in a Statistics class, problems relating to permutation and combination were found with the students.

Sukoriyanto et al. (2016) showed that students make a mistake in understanding the problems that resulted to a mistake when planning the problem's solution. They too made a mistake in rechecking the given information in the problem. All of this information generally confirms that difficulties exist in problem-solving. Driven by interest and curiosity, this study specifically identified the difficulties that are particular to the males and those that relate to the females. Moreover, with the K-12 curriculum, the study compared the encountered problem-solving difficulties between the STEM-related and the non-STEM-related academic programs.

Many studies, which can be observed in publications and other research-dissemination platforms, have already looked at the various ways of coping with the struggles relating to Mathematics. Generally, these coping strategies come in two forms: problem-focused and emotion-focused. Problem-focused coping strategies are efforts to reduce stressful circumstances, while emotion-focused strategies are efforts to regulate the emotional consequences of stressful events (Folkman & Lazarus, 1980; 1985).

Coping with strategy preferences of the individual depend on the area in which he or she experiences the difficulty. One study maintained that problem-focused strategies are most preferred by students in the Western societies (Ader & Erkin, 2012; Lazarus, 1993). A study by Rioveros (2013) revealed otherwise. Tension reduction and emotional engagement, both of which are emotion-focused coping strategies, were the coping strategies most preferred by the respondents, and seeking social support, which is a problem-focused coping strategy, was the least employed.

The information presented comprises the strategies generally utilized by students in managing their painful or difficult moments relating to Mathematics. The desire to unravel the strategies classified by gender and by academic program pushed the study to employ a survey questionnaire that elicited the students' most preferred coping strategies.

While many research projects deal with the difficulties and the coping mechanisms in Mathematical problem-solving, there is conversely a dearth of studies that show the relationships between difficulties and coping strategies via sex and via the academic program. Taking into account this gap in the literature, this article is directed towards developing models that are based on the difficulties

and coping strategies of students in Mathematical problem-solving, and how these are related to the students' sex and academic programs. Ultimately, these models are expected to effectively respond to the struggles of students, when it comes to accomplishing problem-solving tasks in Mathematics.

2. The Literature Review

This section starts by discussing the different kinds and reasons for students' problem-solving difficulties, and how these could be connected to one's sexual orientation. The discussion then transitions to the varied ways students employ to cope with their difficulties. It is also explained how coping strategies can be influenced by one's sex and academic program. Finally, this section concludes with explaining how model-building could serve as an educational intervention to address the gaps and the issues identified.

2.1 The Current Status of Mathematics Education

The majority of people would argue that Mathematics is a subject in which students struggle to comprehend and solve mathematical word problems. In fact, several studies support this claim. The Grade 12 students of Lopez (2008) appeared to have an understanding of Mathematics that does not extend much beyond problem-solving with whole numbers. It is to be emphasised that senior high school graduates must have already acquired the knowledge on the different sets of numbers; and this knowledge is not only confined to whole numbers. This situation may have contributed to the downward trend of achievement levels and the survival rates of elementary and high school students, based on the National Achievement Tests (NAT) from 2005 to 2010, that is, from having a mean percentage score (MPS) of 49.26 to 47.40 in 2008-2009 and down to 46.30 in 2009-2010 (Ronda, 2011).

In support of this information, the study of Banilower et al. (2013) revealed that the performance of Philippine students in the international standardized examination in Mathematics and Science is generally classified as being low.

2.2. Problem-Solving Difficulties

Difficulties in solving Mathematical problems are mainly due to the lack of mathematical skills. Polya (1945) characterized the difficulties in each of the four phases as follows. There is a difficulty in understanding the problem, if one cannot identify the type of problem; while the known and the unknown information, cannot recall facts or concepts, cannot define the terminologies and notations used, and cannot rephrase the problem in one's own words. There is a difficulty in devising a plan, if one cannot draw a picture, tables or charts out of the information; if one is unable to transform problems into mathematical sentences; and if one cannot look for patterns.

If one cannot work with the systematic-working procedure (computational process) in solving the problem in ensuring its accuracy, then one is struggling with carrying out the plan, and if one is unable to evaluate the correctness of the obtained solution that would ensure consistency with the facts of the problem, then he or she has a problem with the looking-back phase.

Several studies confirm the struggles of students in the different phases. Ferguson's (1980) study revealed reading, which is a component of understanding the problem, was the single greatest problem in learning Pre-Calculus Mathematics in college. He also added that reading should not simply mean the ability to pronounce the words or attach names to the symbols, but also the ability to comprehend the material. This belief was further strengthened by a study conducted by Pearce and his colleagues (2013), where it was revealed that the greatest percentage (45%) of his respondents had problems with reading and understanding the problem. Only one cited the problem on computation, while the remaining percentages accounted for the rest of the phase difficulties.

On the other hand, Dela Cruz and Lapinid (2014) revealed that translating worded problems into mathematical symbols was the single greatest difficulty for students. This is due to carelessness, lack of comprehension, interchanging values, and to the unfamiliar words used in the problem. In addition, it was found in a study involving the subject of Physics that the students were unable to remember the relevant equations (Reddy & Panacheroensawad, 2017). In solving those problems that involved derivatives, Nikmah et al. (2019) also discovered that students struggle to devise a planning phase. This was evident when the students tried to seek the maximum value when applying the concept of the first derivative of an algebraic function. The reasons behind this difficulty include the lack or the inadequacy of exercises during classes, lack of understanding the fundamental basics, poor mathematical skills in the necessary understanding of the problem, lack of motivation and inexperienced teachers, poor comprehension skills in definitions, the laws and the basic principles of physics, in addition to the lack of materials in problem-solving.

These difficulties, as discovered by Sukoriyanto et al. (2016), were also evident in a Statistics class, when they were attempting to solve the problems relating to permutation and combination. The students committed an error in understanding the problems that resulted in an error in planning the problem's solution and likewise, this led to an error in rechecking the given information in the problem. This proves that poor mathematical skills and that the lack of understanding the problem comprise the major obstacles in the domain of problem-solving skills.

In other Mathematics-related courses, like Chemistry, some students could correctly solve problems without being able to represent the reactions with an illustration (Nurrenberg & Pickering, 1987; Sawrey, 1990, as cited in Finney, n.d.). This ability of the student falls under the "carrying out the plan" (computational) strategy. They were good at this stage; but they had difficulties involving the "devising a plan" phase. Meanwhile, carrying out the plan and looking back were found to be the major phase difficulties in solving mathematical problems, based on a study conducted by Siniguian (2017).

The inability to translate problems into mathematical equations and the inability to apply mathematical concepts and principles correctly, were the reasons for these phase difficulties. These difficulties were also evident in describing the problem-solving skill of senior high school students of a certain high school in a

foreign country. By administering PISA test items, the results showed a very low category for both devising a plan (DP) and looking back (LB) phases, as well as a medium category for carrying out the plan (CP) phase (Arfiana & Wijaya, 2018).

Difficulties in accomplishing problem-solving tasks may also be affected by the sexual orientation of an individual. Between the two sexes, Ganley (2018) observed that there are more female respondents who encountered difficulties in each phase of problem-solving than did the male respondents. This could be attributed to the female's low levels of confidence in their Mathematical skills than with males.

2.3. Students' Coping Strategies

The term "coping" refers to the thoughts and actions, to which one resorts, when dealing with a stressful situation (Cliche, 2017). Some coping strategies, however, are not as helpful as others. While positive coping strategies give opportunities to actively work towards solving the problems, negative coping strategies make anyone wear down over time; and they often aggravate the situation. Ideally, positive coping strategies include listening to music, going out with a friend, discussing situations with a friend, making an action plan to solve a problem, or seeking counselling to deal with stress; whereas negative coping strategies involve criticizing oneself, yelling at friends, taking a recreational drug, becoming aggressive, or simply avoiding friends and family. Anybody can become stressed for various reasons in different fields and situations; consequently, we need to choose the appropriate coping strategy.

Folkman and Lazarus (1985; 1980) developed and devised a measure called the *Ways of Coping*, which consists of a series of predicates, each portraying a coping action that people sometimes engage in when under stress. They categorized coping strategies into two categories – problem-focused and emotion-focused.

- a) *Problem-focused coping* is generally viewed as an adaptive mode of coping that involves actively planning or engaging in a specific behavior, in order to overcome the problem that is causing distress (Folkman & Lazarus, 1985). The examples of problem-focused coping include planned problem-solving, confrontive/active coping and seeking social/instrumental support, such as friends, families, supervisors and mentors.
- b) *Emotion-focused coping* involves attempts to regulate the emotions evoked by the occurrence of a stressful situation; and it can be considered active or avoidant (Holahan & Moos, 1987; Ryan, 2013). Also, emotion-focused coping may involve the use of behavioral and/or cognitive strategies, such as receiving emotional support from friends and family and positive reframing (Ogden, 2004; Ryan, 2013).

How do the students cope with their stressors? There are a variety of these coping strategies, some are better and more effective to students' learning than others. The following literature illustrates the strategies used by the respondents when confronting their stresses. The respondents of Kahraman and Sungur (n. d), as cited in Rioveros (2013) stated that they cope with their difficulty in three stages. The first involved students defining the event as an obstacle to their goals. Then,

they think of the possible strategies to handle the negative event, and choose one among them. The last stage involves students applying the chosen solution.

Moreover, an examination of the experiences of stress and the coping strategies of high school students in a university (Baluyou, 1999; Rioveros, 2013) revealed that self-control, distancing, and planned problem-solving were useful and effective coping strategies. Problem-focused coping tends to predominate, when people feel that something constructive ought to be done, whereas emotion-focused coping tends to predominate, when people feel that the stressor is something that must simply be endured (Carver, et al., 1999; Folkman & Lazarus, 1980; Ghana, 2011). Due to their action-orientation, problem-focused coping strategies are more highly valued in Western societies (Ader & Erkin, 2012; Lazarus, 1993).

2.3.1. *Gender and Coping*

Based on sex-typed predispositions, men and women adopt different coping strategies, a theory that has been frequently explored. Men would be expected to utilize problem-focused coping more than women. Men used significantly more direct actions (Rapson, 1990), and less frequently used active-behavioural avoidance and emotion-focused coping (Billings & Moos, 1984, as cited in Rapson, 1990; Eschenbeck, et al., 2002). Women, on the contrary, are expected to use more emotion-focused coping than do men (Brougham et al., 2009; Hammermeister & Burton, 2004; Kaiseler et al., 2012). They tend to use more distraction, catharsis, seeking social support, relaxation and other types of coping (Rapson, 1990; Stone & Neale, 1984), in addition to information-seeking and emotional discharging (Billings & Moos, 1984, as cited in Rapson, 1990).

Tamres and colleagues (2002) revealed that women are more likely to use strategies that involve verbal expressions to others or the self—than to seek emotional support, ruminate about problems, and use positive self-talk.

2.3.2. *Academic Programs and Coping*

A few studies reveal that students of different courses encounter varied mathematical difficulties, hence, with varied coping strategies. In a study involving BEED (Bachelor of Elementary Education) and BSEd (Bachelor of Secondary Education) students, it was disclosed that listening attentively to the teacher was the most significant coping mechanism, if one had no focus on Math tasks and one was easily distracted by external factors (Bagasol et al., 2015). The use of diagrams and pictures out of the problems and engaging in leisure activities were found to be the least-significant coping mechanisms for the students enrolled in BEED and BSEd courses, respectively.

In the field of health and medicine, nursing students experienced different levels of stress that include the caring for patients, assignments and workloads, and negative interactions with staff and faculty; thus, they utilized problem-solving strategies, such as developing objectives to resolve problems, adopting various strategies to address problems, and finding the meaning of stressful events (Labrague et al., 2016), which were all problem-focused coping strategies.

Finalyson (2014, as cited in Quan, 2015), maintained in his survey paper that relaxing, building self-confidence, practice, studying and doing one's homework

and getting help from others were the most preferred problem-focused coping strategies. On the contrary, among general education students, active coping, which is another form of problem-focused coping strategy, was revealed as being the most frequently used strategy (Okoro, 2018).

2.4. Model-Building

Model-building provides a framework that guides the researcher in addressing the objectives of this study. Some empirical studies have already employed the model-building framework as their research design; and they have found it efficient and effective in attaining research aims. Houghton and his colleagues (2012), through the model that they developed, suggested that effective emotion regulation and self-leadership, mediated through positive affect and self-efficacy have the potential to facilitate stress-coping among students. In another research context, challenged with technology-education students, Ernst (2009) focused on the development of problem-solving models that employ societal, cultural, and economic considerations. The results revealed no apparent effect on the initial component selection of problem-solving modelling, whether challenged with environmental or manufacturing issues. In the area of combinatorics, a model of student's combinatorial thinking, related to counting, was developed by Lockwood (2013). This model elaborated on the relationships between formulas/expressions, counting processes and sets of outcomes. Likewise, it served as an initial attempt for providing ideas and common language that researchers could utilize in evaluating their own students' combinatorial thinking and activities.

3. The Research Methodology

Figure 1 shows the model-building framework that was followed in conducting this study. It employed a design-research approach with four components—analysis, development, implementation, and validation. The data were gathered by administering a problem-solving test and a coping-strategy questionnaire. The study is generally descriptive that employed quantitative and qualitative analysis.

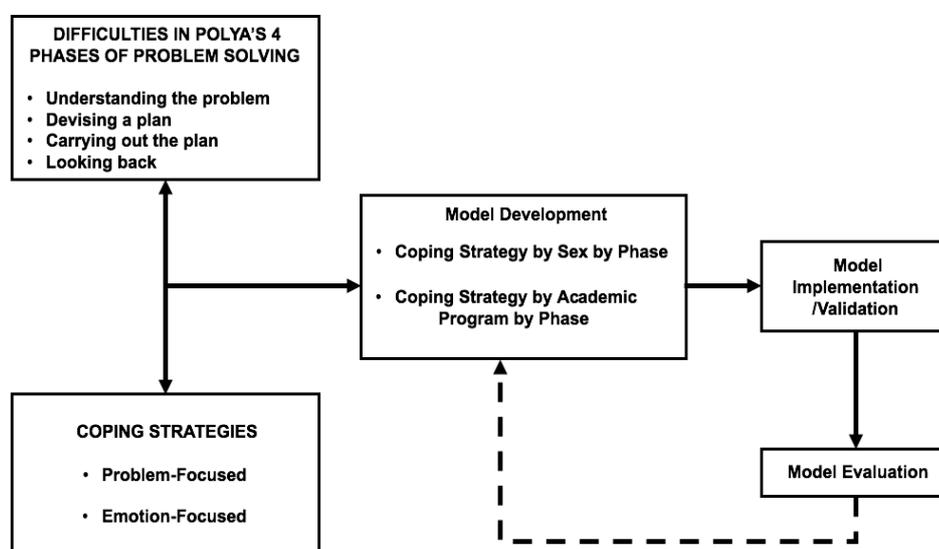


Figure 1: The Model-Building Framework of the Study

The Analytical Stage. This stage dealt with the analysis of the Mathematics problem-solving difficulties of the students by administering a problem-solving test. Likewise, coping strategies were elicited from the respondents by requesting them to answer the Coping -strategy Questionnaire. Two difficulties in each of the problem-solving phases were revealed; and the students preferred the Problem-focused coping strategies for dealing with with their difficulties.

The Model-Developmental Stage. Two models associating the Mathematical problem-solving difficulties and coping strategies of the students were generated and developed, namely: the coping strategies by sex by phase model, and the coping strategies by the academic program of the phase model. These models were linked with the students' sexual orientations and academic programs.

Model Implementation. This stage validated the models developed by engaging the students (validation group) through the administration of a similar problem-solving test. Purposive sampling was employed in validating the models. Factors, such as the availability of the respondents and the matching of coping strategies ,as presented in the models developed, were taken into consideration.

The Model-Evaluation Stage. This stage assessed and determined whether the problem-solving difficulties of the students were addressed, or not, through the coping strategies, as modelled. A decrease, or a total eradication of the pre-identified difficulties, concluded the effectivity of the models developed, that is, they could address the difficulties of the students in their problem-solving encounters through their coping strategies. A total of 425 respondents participated in the study. The distribution of these respondents, based on their sex, and on the academic program is clearly presented in Table 1. They were enrolled in Mathematics in the Modern World, offered in a certain Philippine university during the first semester of the school year 2018-2019. The respondents belonged to the same year level, within the 18-19 year-old age bracket; and they were considered to be the first graduates of the K-12 curriculum.

Table 1: Distribution of respondents by sex and academic program

Academic Programs	Number of Classes	Number of Males	Number of Females	Total
STEM-related academic programs				
BS-Agricultural and Biosystems Engineering	2	28	43	71
BS-Chemical Engineering	1	10	12	22
BS-Civil Engineering	3	67	46	113
BS-Mathematics	1	5	21	26
BS-Meteorology	1	9	8	17
BS-Nursing	2	15	62	77
Subtotals		134	192	326

Non-STEM-Related academic programs				
BA-Communication	1	8	24	32
BS-Economics	1	11	25	36
BS-Sociology	1	8	23	31
Subtotals		27	72	99
OVERALL TOTAL		161	264	425

The study needed two independent groups – the model -development group and the model-validation group. The grouping scheme applied the 70-30 scheme of partitioning the students. This scheme, according to Pete (2017), is arbitrary. However, the more respondents that are included in the development stage (70%), the better the developed model. Of the 425 respondents, 297 respondents represented the 70%; and they were included in the model development with the distribution of respondents by sex and academic program, as found in Table 2. This sum was identified through random sampling, specifically done through a table of random numbers generated by stattrek.com. The selected samples, however, had their final say by their participation in this study.

Table 2: Distribution of respondents by sex and academic program in the model-developmental stage

Course	Male	Female	Total
STEM-Related academic programs			
BS-Agricultural and Biosystems Engineering	22	28	50
BS-Chemical Engineering	8	7	15
BS-Civil Engineering	48	31	79
BS-Mathematics	3	15	18
BS-Meteorology	8	4	12
BS-Nursing	11	43	54
Sub-totals	100	128	228
Non-STEM-related academic programs			
BA-Communication	5	17	22
BS-Economics	9	16	25
BS-Sociology	4	18	22
Subtotals	18	51	69
TOTALS	118	179	297

Meanwhile, the developed models were validated by the remaining 128 respondents that represented the 30% of the total respondents, as can be seen in the distribution in Table 3. Their participation was primarily aimed at testing whether the developed models are appropriate, and could eventually address the problem-solving difficulties of the students in the case samples.

Table 3: Distribution of respondents by sex and academic program in the model validation stage

Course	Male	Female	Total
STEM-Related academic programs			
BS-Agricultural and Biosystems Engineering	8	13	21
BS-Chemical Engineering	3	4	7
BS-Civil Engineering	20	14	34
BS-Mathematics	2	6	8
BS-Meteorology	3	2	5
BS-Nursing	4	19	23
Subtotals	40	58	98
Non-STEM-related academic programs			
BA-Communication	3	7	10
BS-Economics	3	8	11
BS-Sociology	2	7	9
Subtotals	8	22	30
TOTALS	48	80	128

3.1. The Research Instruments

This study utilized two research instruments, in order to collect the data from the respondents. The first one was a problem-solving test, which aimed to determine the problem-solving difficulties of students in Mathematics. The second instrument was the coping-strategy questionnaire, which is appended to the last part of the problem-solving test. This instrument was used to identify the coping strategies deployed by the students, when attempting to deal with their difficulties.

3.1.1. The Problem-Solving Test

This test facilitated the identification of the problem-solving difficulties of the students. The test items were routine problems, which were applications in Algebra, such as problems of age, geometry/dimensions, work, mixture, investment/interest, motion, number relations and of money. Students' solutions were assessed by the researchers, which were then counterchecked by two of their validators. It was pilot-tested and had a Cronbach's alpha reliability of 0.79, which was acceptable.

3.1.2. The Coping-Strategy Questionnaire

This questionnaire facilitated the identification of the common coping strategies of the students in solving mathematical problems. It was appended to the last part of the problem-solving test. The students were asked to share their past experiences, particularly in problem-solving situations. They were requested to share how they had managed their difficulties through their coping strategies.

4. The Research Results

This section discusses the research results, starting with the identification of the students' problem-solving difficulties. It then proceeds with the elaboration on students' preferred coping strategies. Lastly, models were developed showing the problem-solving difficulties, by sex, by phase and the students' problem-solving difficulties by academic program by phase. In this section of the paper, it should

be noted that acronyms were used to represent the four problem-solving phases – understanding the problem (UP), devising a plan (DP), carrying out the plan (CP), and looking back (LB).

4.1. Problem-Solving Difficulties

Two common difficulties in each of the four phases were revealed. The difficulties were coded with prefixes indicative of the problem-solving phase. These codes were introduced by the researchers themselves. It can be seen in Table 4, that the students encountered difficulties in the different phases of problem-solving, as supported by studies from Siniguan (2017), as well as those of other scholars.

Table 4: Problem-solving difficulties in the different phases

Problem-Solving Phases	Identified Difficulties	Code
Understanding the Problem (UP)	1. Inability to distinguish the known from the unknown information	U1
	2. Inability to identify the type of problem and recall basic facts	U2
Devising a Plan (DP)	1. Inability to transform a problem into a mathematical equation.	D1
	2. Inability to draw tables/charts out of the information and organize information and connect to a concept.	D2
Carrying Out the Plan (CP)	1. Inability to completely perform the working procedure systematically and accurately.	C1
	2. Inability to start with the computational process.	C2
Looking Back (LB)	1. Inability to complete the checking procedure.	L1
	2. Inability to start the evaluation of the correctness of the obtained solution.	L2

The following are a few examples of the students' solutions, illustrating some of their difficulties in each of the phases.

4.1.1. Understanding the Problem Phase (UP)

Figure 2 shows the student's inability to distinguish the known from the unknown information. It can be clearly observed in the figure that the student merely lifted the words/phrases, as stated in the problem.

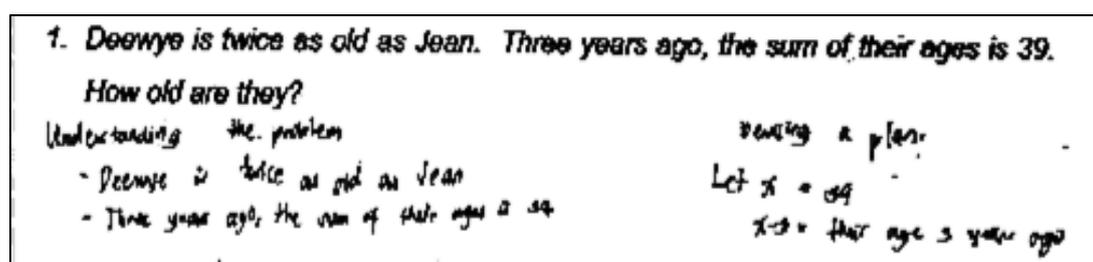


Figure 2. Solution of BS-ABE

Figure 3 presents the student's immediate manipulation of his or her working equation without trying to distinguish the given/known and the unknown information of the problem. He or she was not able to identify the type of problem and to recall the basic concepts, thus, he/she left the space provided blank.

12. Ellah has exactly P200 in P5 coins and P10 bills. He has twice as many P10 as P5. How many of each does he have? (Petilos, 2002)

12. ~~200~~ $x + y = 200$ $x = 20$
 $5x + 10y = 200$ $y = -10$

$(5 \times 20) + (10 \times 10) = 200$

$100 + 100 = 200$

20 five peso coins &
 10 ten peso bills

Figure 3: Solution of BA-COMM-1

Figure 4 shows the student's inability to distinguish the unknown information in the problem; and he/she just lifted the exact words used in the problem.

2. In consecutive turns of a Monopoly game, Stacy first paid P8,000.00 for a hotel. She then lost half her money when she landed on Boardwalk. Next, she collected P2,000.00 for passing GO. She then lost half her remaining money when she landed on Illinois Avenue. Stacy now has P25,000.00. How much did she have just before she purchased the hotel? (Aufmann, 2013)

Known: P8,000 first paid
 - $\frac{1}{2}$ of money ^{when} lost when she landed in boardwalk
 - she collected 2000 for passing GO
 - lost $\frac{1}{2}$ of her remaining money
 - 25,000 final money

revising the plan

~~Stacy now has P25,000.00. How much did she have just before she purchased the hotel?~~

$x - 8000 = \text{hotel}$
 $\frac{x - 8000}{2} = \text{lost}$
 $\frac{x - 8000}{2} + 2000 = \text{passing GO}$
 $\frac{x - 4000}{2} + 2000 = 25000$

Figure 4: Solution of BSCE-B1

Looking at the solution of Figure 5, the respondent completely left the space provided for understanding the problem phase. The student did not write anything about the problem's given and unknown information; because s/he was not familiar with the type of problem and could not recall basic facts.

19. Seven times a 2-digit number is equal to 4 times the number obtained by reversing the digits. The difference between the digits is 1. Find the number.

19.

$$7(1a) = 4(21)$$

$$\downarrow \qquad \qquad \downarrow$$

$$84 = 84$$

$$a - 1 = 1$$

Figure 5: Solution of BSN-A2

4.1.2 Devising a Planned Phase (DP)

One can easily check that the student was unable to transform the problem into a mathematical equation in Figure 6.

3. A 12 cm by 16 cm rectangular piece of cardboard has a 2cm by 2cm square cut out of each corner. Then the sides are folded up to make an open box. What is the volume of the box?

UNDERSTANDING THE PROBLEM

Known: → 12 cm by 16 cm rectangular piece of cardboard

→ 2cm by 2cm square cut out of each corner

Unknown: → volume of the box

• Devising a plan:

Let $12x + 16x =$ rectangular

$2^2 =$ square cut

$4x =$ side of square

Working equation

$$12x + 16x - (2)^2 = 4x$$

DP-LB

Figure 6: Solution of BS-Econ A16

Figure 7 shows how the student worked well for the given situation, but was not able to formulate the mathematical equation that applied to the distance/motion problem. A diagram could have helped the student to analyze the situation.

7. Two cars leave a town and travel in opposite directions. One car travels at the rate of 45 kph, and the other at 55 kph. In how many hours will the two cars be 350 kilometers apart?

① Type: Number problems
 Unknown: hours the two cars will be 350 km apart
 Known: car A = 45 kph
 Car B = 55 kph

② DP
 Let x = no. of hours
 Working equation:

③

45 km	}	1st hour
+ 55 km		
100 km		
+ 100 km		⇒
200 km → 2nd hour		
+ 100		
300 km → 3rd hour		
+ 50		
350 → 3rd hour + 30 minutes		

→ 3 hours and 30 minutes

LP

Figure 7: Solution of BS-Meteo I

Figure 8 shows the solution of the student, who incompletely formed the mathematical equation for the stated problem. Incomplete in a way that s/he missed an expression to make the mathematical equation feasible.

START HERE. Solve each problem near illustrate each of the four phases of pro

1. Deewye is twice as old as Jean. How old are they?

Understanding the Problem
 - Deewye is twice as old as Jean
 - 3 yrs ago, the sum of their age is 30

Devising a Plan
 x = Jean
 $2x$ = Deewye

$$2x + x - 3 = 39$$

Figure 8: BA-Socio I

Figure 9 shows that s/he was able to distinguish the unknown from the known information, however, s/he was unable to formulate the working equation.

9. Jenina owns a pet shop that specializes in tropical fishes. In April, Jenina doubled the number of fish she had on hand and then sold 30 of them. In May, she tripled the number of fish she had on hand, and then sold 54 of them. In June, she quadrupled the number of fish she had, and then sold 72 of them. She now had 48 fish left. How many fish did she start with? (Petilos, 2002)

4) I - known: In April, Jenina doubled the num. of fish then sold 30
 In May, she tripled the num. of fish then sold 54
 In June, she quadrupled the num. of fish then sold 72
 48 fish left
 Unknown: how many fish did she start with?

II. Let x = be the num. of fish
 $2x - 30$ = in April
 $3x - 54$ = in May
 $4x - 72$ = in June

Working Equation:
 $2x - 30 + 3x - 54 + 4x - 72$

III.
 $2x - 30 + 3x - 54 + 4x - 72 = 48$
 $2x + 3x + 4x = 48 + 30 + 54 + 72$
 $\frac{9x}{9} = \frac{204}{9}$
 $x = 23$

DO NOT
 $2x - 30$
 $3(2x - 30) - 54$
 $4(6x - 60 - 54) - 72$
 $24x - 240 - 216 - 72 = 48$
 $24x = 48 + 240 + 216 + 72$
 $24x = 576$
 $x = 24$

Figure 9: Solution of BS-CHEM E14

4.1.3. Carrying out the Planned (CP) Phase

In Figure 10, it can be observed that the mathematical equation formed is correct, but the student was not able to completely perform the working procedure accurately.

5. How much pure acid should be mixed with 2 gallons of a 40% acid solution in order to get a 70% acid solution?

Student
Approach + VIP

Known: there are 2 acid solutions
40% and 70%

Mixture is 70% acid solution
There are 40% in 2 gallons

DAP



Working equation:
 $1x + 4(2) = .70(x+2)$

Carrying the plan:

$$x + .8 = .7x + 1.4$$

$$x - .7x = 2 - .8$$

$$\frac{0.3x}{0.3} = \frac{1.2}{0.3}$$

$$x = 4$$

CP-10

Checking Back:
 $x = 4$ gallons

Therefore 4 gallons of 100% acid solution is needed. $\$$

Figure 10: Solution of BSCE-A2

It can be observed that the student (Figure 11) was unable to start with the computational process because s/he was not able to form the mathematical equation.

4. Jonathan can finish an accounting work in 8 hours. Carl can finish the same work in 6 hours. After 2 hours of working together, Jonathan left Carl for lunch and Carl finished the job. How long does it take Carl to finish the job?

Understanding the Problem

- Jonathan can finish an accounting work in 8 hrs.
- Carl can finish the same work in 6 hrs.
- After 2 hrs, Jonathan left Carl for lunch
- Carl finished the job.

Unknown: hours that Carl finished the job

Carrying out the Plan

Let $x =$

Figure 11: Solution of BS-ABE-B23

The difficulty of performing the computational process coincides with the findings of the study of Siniguan (2017) and Dela Cruz and Lapinid (2014), in which they investigated the difficulties experienced by the third-year college students in solving Mathematical problems. The study revealed that the difficulties are in the inability to translate into mathematical formulae (DP) that which consequently affected the student's computational process (CP), and the inability to use correct mathematics (CP).

4.1.4. The Looking-Back Phase (LB)

Figure 12 presents the procedure that went well; but the student was not able to complete the checking procedure.

8. The first of three numbers exceeds twice the second number by 4, while the third number is twice the first. If the sum of the three numbers is 54, find the numbers.

wf, DP

solution =

$$\begin{aligned} x + y + z &= 54 \\ y &= 2x + 4 \\ z &= 2x \end{aligned}$$

$$2x + 4 + 2x + 2x = 54$$

$$6x + 4 = 54$$

$$6x = 54 - 4$$

$$6x = 50$$

$$x = \frac{50}{6} = 8\frac{1}{3}$$

$$y = 2(8\frac{1}{3}) + 4 = 16\frac{2}{3} + 4 = 20\frac{2}{3}$$

$$z = 2(8\frac{1}{3}) = 16\frac{2}{3}$$

10

Figure 12: Solution of BSN-A1

In Figure 13, the student succeeded in performing the first three steps of Polya's (1945) four phases, although s/he was not able to start the evaluation of his or her obtained solution.

6. Xander invested P35,000.00 in a savings account that pays 4% simple interest. How much will he earn after 3 years? What will the new balance be?

Known : Xander invested P35,000
savings account that
pays 4% simple interest.

Unknown : earn after 3 years.

Investment = P35,000
Rate = 4%
Time = 3 yrs.

Let x be the new balance after 3 years.

$$x = P35,000 + P35,000(0.4)(3)$$

$$x = P35,000 + P35,000(1.2)$$

$$x = P35,000 + P9,200$$

$$x = P37,200$$

Figure 13: Solution of BS-Econ-15

In Figure 14, the student was able to recheck/re-evaluate the derived value; but it was not consistent with the facts of the problem.

6. Xander invested P35,000.00 in a savings account that pays 4% simple interest. How much will he earn after 3 years? What will the new balance be?

I. Xander invested P35,000 in a savings account that pays 4% simple interest.
 Unknown: X How much will he earn after 3 years?

II. $(P35,000 \times 0.04) + P35,000 = P36,400$ (3)

III. $(P35,000 \times 0.04) + P35,000 = P36,400$ (3)

IV. $X = (P35,000 \times 0.04) + P35,000$ for 3 years
 $X = P36,400$
 $Y = P36,400 \times (3 \text{ years})$
 $Y = P109,200$

Therefore Xander's earning after 3 years is P109,200.00
 And his new balance is P144,200.00

$Z = P109,200 - P35,000 = P74,200$
 $Z = \text{new balance}$
 $Z = Y - X$

Figure 14: Solution of BS-ABE-A6

Figure 15 showed that the procedures went well, as can be seen from the solutions; however, s/he was not able to check whether the conditions given in the problem were satisfied or not.

8. The first of three numbers exceeds twice the second number by 4, while the third number is twice the first. If the sum of the three numbers is 54, find the numbers.

solution -
 $x + y + z = 54$
 $x = 2y + 4$
 $z = 2x$

$2y + 4 + y + 2x = 54$
 $3y + 2x = 50$
 $x = 2y + 4$

$3y + 2(2y + 4) = 50$
 $3y + 4y + 8 = 50$
 $7y = 50 - 8$
 $7y = 42$
 $y = \frac{42}{7} = 6$

$x = 2(6) + 4 = 12 + 4 = 16$
 $z = 2(16) = 32$

Figure 15: Solution of BSN-A1

A summary of the common difficulties classified, according to sex and the academic program is presented in Table 5. It can be gleaned from the table that both males and females experienced the same type of difficulty in every phase of the problem-solving.

Table 5: Common problem-solving difficulties by sex and by phase

Problem-Solving Phases	Sex	
	Male	Female
Understanding the Problem (UP)	U1	U1
Devising a Plan (DP)	D1	D1
Carrying Out the Plan (CP)	C1	C1
Looking Back (LB)	L2	L2

Similarly, it can be seen in Table 6 that the majority of the students in the STEM-related academic programs had difficulties in U2, D1, C1 and L2; while the majority of the students in the non-STEM related academic programs had difficulties in U1, D1, C1 and L2.

Table 6: Common problem-solving difficulties by academic program by phase

Problem-Solving Phases	Academic Programs								
	STEM-Related						Non-STEM-Related		
	BS-ABE	BSCE	BS-ChE	BSM	BS-Met	BSN	BA-Com	BS-Econ	BS-Soc
Understanding the Problem (UP)	U1	U1	U2	U2	U2	U2	U1	U1	U1
Devising a Plan (DP)	D1	D1	D1	D2	D1	D1	D1	D1	D1
Carrying out the Plan (CP)	C1	C1	C1	C2	C1	C2	C1	C1	C1
Looking Back (LB)	L2	L2	L2	L2	L2	L2	L2	L2	L2

4.2. Coping Strategies in the Different Phases of Problem-Solving

There were 43 strategies that were elicited in the coping-strategy questionnaire. Each coping strategy was coded by using acronyms indicative of the problem-solving phase, where it belonged. For instance, the acronym UP1 is used to refer to the first strategy in the understanding of the problem phase (UP). Of the 43 identified strategies, 32 were problem-focused and 11 were emotion-focused. There were 10 strategies each, for the UP and the DP phases respectively, 12 for the CP phase and 11 for the LB phase.

Table 7a: Coping strategies in the “understanding the plan phase”

Understanding the Problem	Coping Strategies	Code
Problem-Focused	recalled and/or applied basic facts/principles/stock knowledge	UP1
	understood fully, analyzed and listed/enumerated all the given information and/or thought critically/logically giving the focus on the problem/needed focus	UP2
	familiarization of terminologies using online references and/or non-online references	UP3
	re-read/re-write the problem and the identified clues	UP5
	rephrase/translated the sentence in one’s own words/grammar construction	UP6
	asked seatmates/friends/teacher/tutor to help explain/solve (assistance)	UP7
	looked for more exercises in books, and read books related to the problem at hand/more exposure	UP8
	reviewed old notes/lectures taught by the teacher	UP9
	listened attentively to the teacher	UP10
Emotion-Focused	ignored	UP4

Table 7b: Coping strategies in the “devising a plan phase”

Devising a Plan	Coping Strategies	Code
Problem-Focused	recalled and/or applied related strategies/concepts previously studied/stock knowledge to real-life situations	DP1
	understood fully, analyzed/thought through critically and pondered on what the formula would be	DP2
	searched online for some strategies/related problems	DP3
	proceeded in creating one’s own strategy/plan/formulas	DP4
	performed trial-and-error with plans	DP5
	organized information expressing the variables and the other numbers connecting them to a concept	DP6
	asked friends/teacher/tutor to help explain/solve (assistance)	DP7
	looked for more exercises in books and read books related to the problem at hand/more exposure/needed more problem-solving exercises	DP8
	needed computing gadgets	DP9
Emotion-Focused	did best to advance the study	DP10

Table 7c: Coping strategies in the “carrying out the plan phase”

Carrying out the Plan	Coping Strategies	Code
Problem-Focused	understood fully, analyzed/thought critically and solved the problem carefully/self-study; applied plan to answer the problem by oneself	CP1
	With the formulas as guides, one was able to make substitutions/computations; but one needed computing gadgets	CP2
	watched YouTube/online applications /tutorials on the process of computations	CP3
	learned/reviewed the process/computations	CP4
	performed trial-and-error approach	CP6
	asked friends/teacher/tutor to help explain further the process/computation/copied from seatmate	CP7
	needed to read more books/references and lots of problem-solving exercises/more practice/ more exposure	CP8
Emotion-Focused	questioned oneself on how to solve it	CP5
	just overcame through positivity	CP9
	shared feelings with someone	CP10
	Ignored	CP11
	Talk and pray	CP12

Table 7d: Coping strategies in the “looking-back phase”

Looking Back	Coping Strategies	Code
Problem-Focused	rechecked/re-evaluated whether the answer was correct	LB1
	understood/analyzed the problem and more/self-study	LB2
	looked for more exercises in books and read books related to the problem at hand/more exposure	LB8
	be objective in formulating the equations	LB4
	performed trial and error	LB5
	needed English-language skills	LB6
	asked friends/teacher/tutor to help explain the whole process/sought assistance from others	LB7
Emotion-Focused	thought that things would get better; thought that one would get mature enough to handle the problems next time, and not get confused with questions that have easy solutions	LB3
	believing in one's own self-onfidence	LB9
	concluded briefly	LB10
	Ignored	LB11

4.2.1. Coping Strategies by Sex and by Phase

Table 8 shows the top three coping strategies utilized by the students in each of the phases. The majority of the students in both sexes revealed that they utilized the same coping strategies for the UP, DP and CP phases. On the other hand, the majority of the female students preferred the coping strategy LB1, while the majority of the male respondents employed LB3 for the males in the LB phase.

These strategies are all classified under problem-focused coping strategies, except LB3, which is an emotion-focused coping strategy.

Table 8: Top three common coping strategies by sex and by phase

Phases of Problem-Solving	Coping Strategies	Sex	
		Male	Female
Understanding the Problem (UP)	Problem-Focused	UP2* UP3 UP8	UP2* UP3 UP5 UP8
	Emotion-Focused		
Devising a Plan (DP)	Problem-Focused	DP3 DP4 DP8*	DP2 DP3 DP8*
	Emotion-Focused		
Carrying Out the Plan (CP)	Problem-Focused	CP1 CP7* CP8	CP1 CP2 CP7*
	Emotion-Focused		
Looking Back (LB)	Problem-Focused	LB1	LB1* LB2
	Emotion-Focused	LB3* LB9	LB3

* The coping strategy utilized by the majority

Table 9a presents the top three common coping strategies of the different academic programs in the STEM track. Across programs, the majority of the students preferred the strategies of UP2, DP8, CP7 and LB1 in each of the different phases, all categorized as problem-focused coping strategies. It is worth noting, however, that the majority of the students in the BS in Civil Engineering, BS in Mathematics and BS in Nursing, applied LB3, which is an emotion-focused coping strategy.

Table 9a: Top three common coping strategies by STEM-related academic Programs by phase

Phases of Problem-Solving	Coping Strategies	Stem-Related Academic Programs						
		BS-ABE	BSCCE	BSCHE	BSM	BSMET	BSN	Majority
Understanding the Problem (UP)	Problem-Focused	UP2* UP5 UP8	UP2 UP3*	UP2* UP3 UP8	UP2 UP3*	UP1 UP2*	UP2* UP5 UP8	UP2
	Emotion-Focused							
Devising a Plan (DP)	Problem-Focused	DP3 DP7 DP8*	DP2 DP3 DP8*	DP4 DP5* DP8*	DP3 DP7 DP8*	DP1 DP2 DP7*	DP1 DP3 DP8*	DP8
	Emotion-Focused							
Carrying Out the Plan (CP)	Problem-Focused	CP1 CP2 CP7*	CP1 CP7* CP8	CP1* CP3 CP7*	CP1 CP4 CP7*	CP1* CP2* CP3	CP1 CP2 CP7*	CP7
	Emotion-Focused							
Looking Back (LB)	Problem-Focused	LB1*	LB1*	LB1* LB8	LB1* LB2*	LB1 LB5 LB7*	LB1 LB2	LB1
	Emotion-Focused	LB3 LB9	LB3* LB9	LB9	LB3*		LB3*	

* Top 3 coping strategies utilized by the majority

For the three non-STEM-related academic programs in Table 9b, students preferred the strategies of UP2, DP8, CP7 and LB3. It is to be noted that LB3 is an emotion-focused coping strategy, which was preferred by the majority of the students in the said academic program.

Table 9b: Top three common coping strategies by non-STEM-related academic programs by phase

Phases of Problem-Solving	Coping Strategies	Non-Stem-Related Academic Programs			
		BA Com	BS Econ	BS-Soc	Majority
Understanding the Problem (UP)	Problem-Focused	UP1 UP2* UP5	UP2* UP3 UP8	UP2* UP3 UP8	UP2
	Emotion-Focused				
Devising a Plan (DP)	Problem-Focused	DP2 DP4* DP6	DP2 DP5 DP8*	DP1 DP3 DP8*	DP8
	Emotion-Focused				
Carrying Out the Plan (CP)	Problem-Focused	CP1* CP3 CP7*	CP1 CP6 CP7*	CP1 CP3 CP7*	CP7
	Emotion-Focused				
Looking Back (LB)	Problem-Focused	LB1* LB7	LB5 LB7* LB8	LB1 LB5 LB7	
	Emotion-Focused	LB3*		LB3* LB9	LB3

* Top 3 coping strategies utilized by the majority

Comparing the data presented above, it can be summarized that the two groups utilized the same coping strategies from the UP phase until the CP phase. The LB phase, on the other hand, shows that the two academic programs preferred dissimilar coping strategies; LB1 for the STEM-related and LB3 for the non-STEM-related programs, respectively.

4.3. Model Development

After careful examination of the associations between and among the variables in this study, the following models were developed.

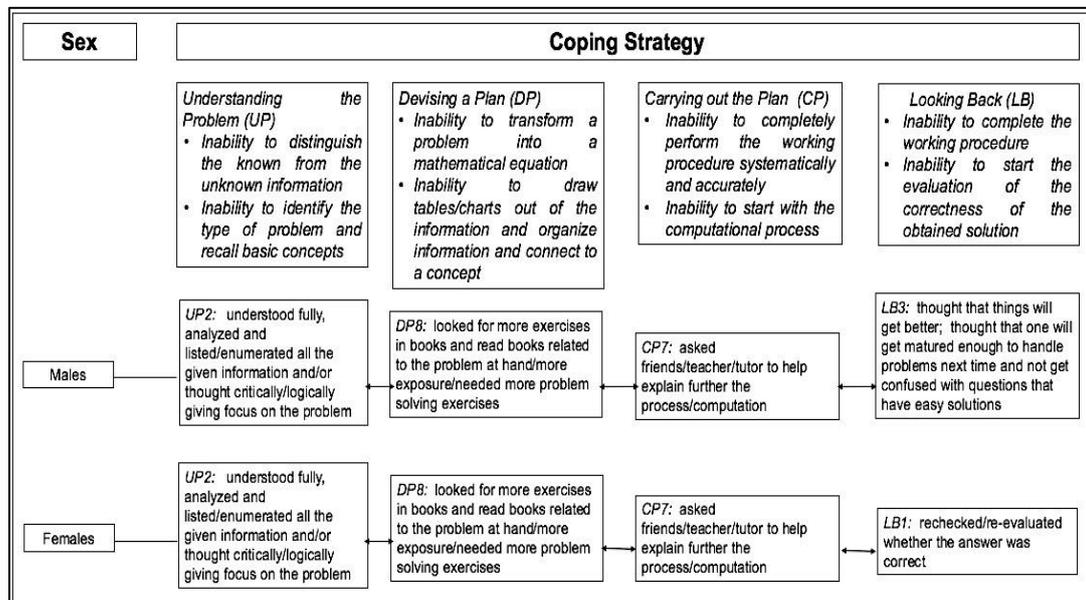


Figure 16: Coping Strategy by Sex by Phase Model

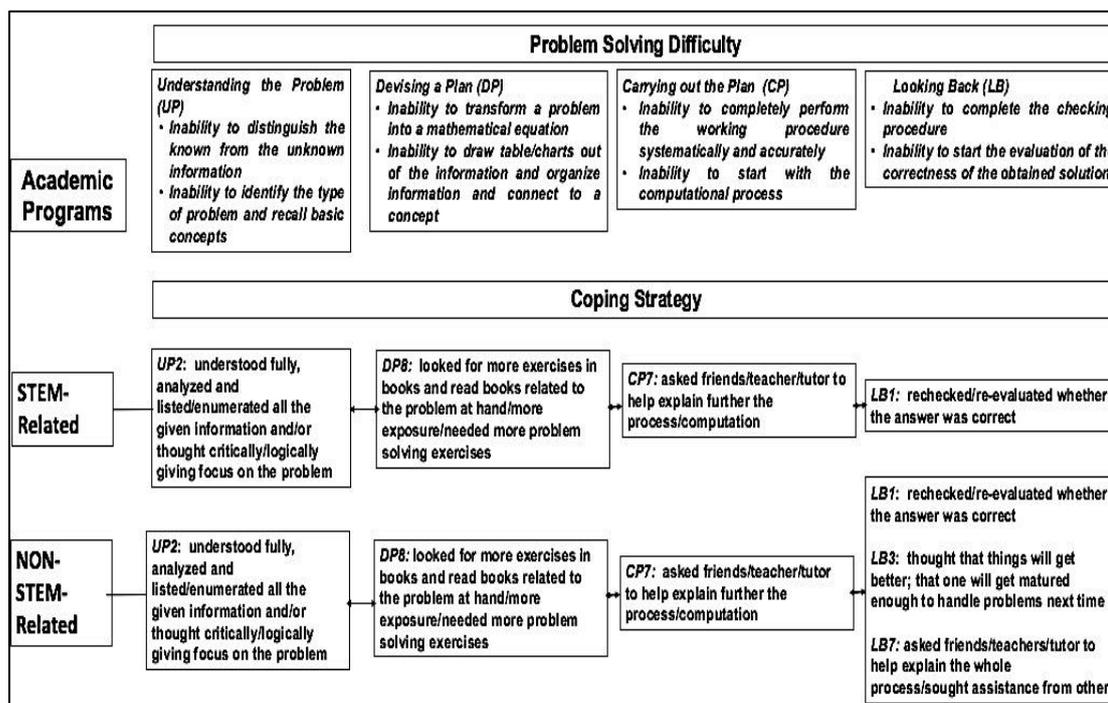


Figure 17: Coping Strategy by Academic Program (in General) by Phase

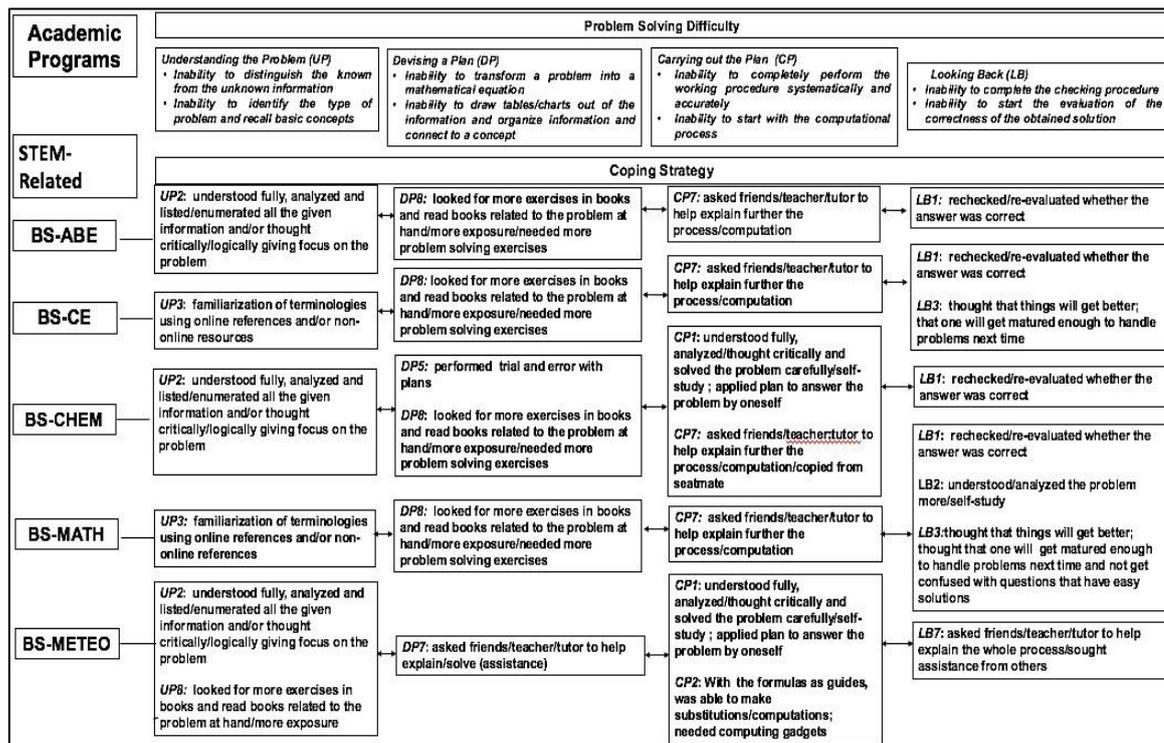


Figure 18: Coping Strategy by Academic Program (STEM-Related) by Phase

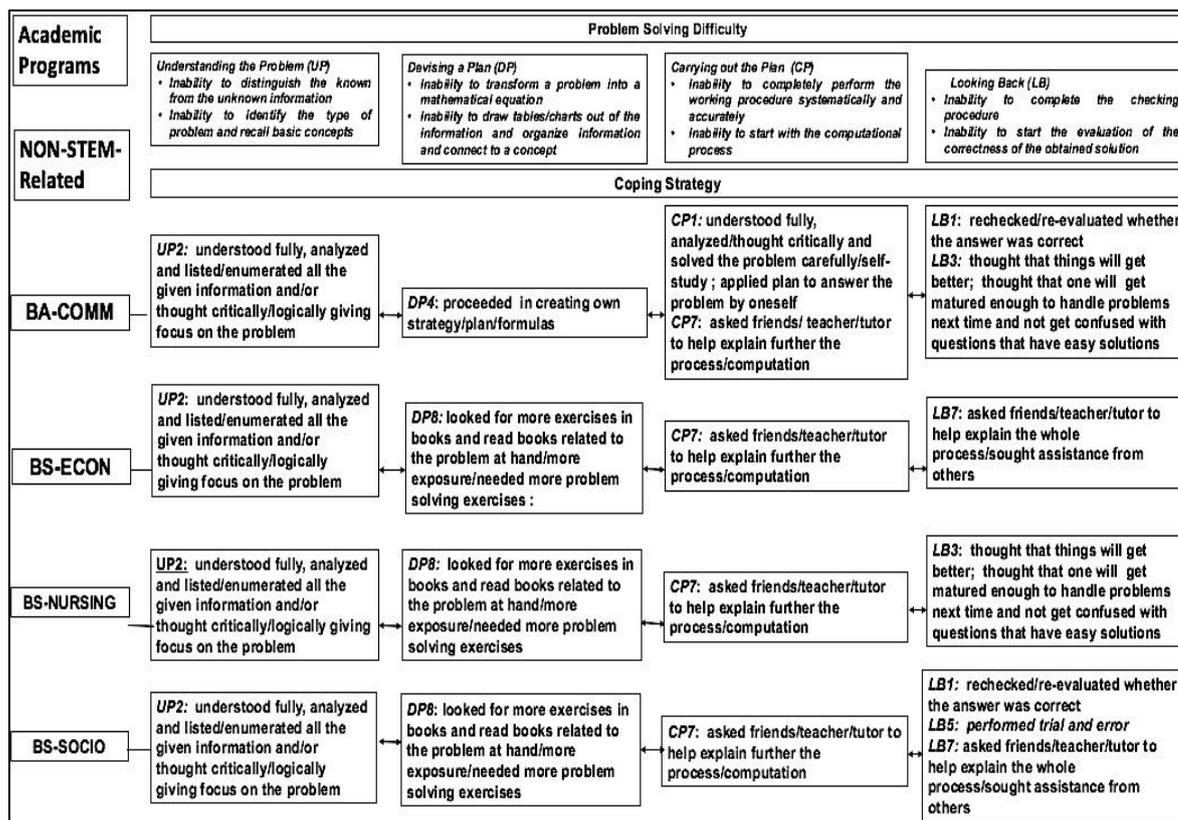


Figure 19: Coping Strategy by Academic Program (non STEM-related) by Phase Model

4.4. Model Validation

Addressing the difficulties of the students through their coping strategies was one of the aims of the study, hence, validation of the models had to be undertaken. Purposive sampling was done to select the respondents that would be included in the validation group; thus, factors like availability of the respondents, together with their coping strategies that matched those presented in the models developed, were taken into account. Eight male respondents and 10 female respondents were sampled for validating the “Coping Strategies by Sex by Phase Model”.

In Figure 20, the pretest of Male #1 had pre-identified difficulties, namely; DP, CP and LB. However, the post-test revealed that there was a reduction in his phase and a difficulty after incorporating the coping strategy UP2. Considering the eight males that were sampled, it can be observed in the post-test that there had been a reduction in their pre-identified difficulties.

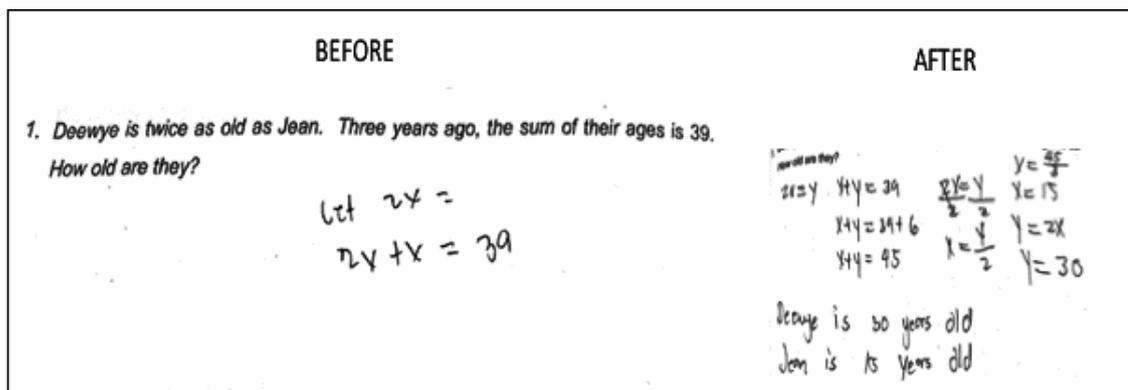


Figure 20: Pre-Post Solution of Male #1
Difficulty/ies: DP, CP, LB;
Coping Strategy/ies: UP2

Focusing on the solution of the Male #2 in the pretest in Figure 21, it can be seen that he was successful in deriving the answers for the requirements of the problem. But after looking for more exercises and reading more books with related problems (DP8), the student was able to check his derived values, and concluded consequently. Hence, the student’s difficulty, which was looking back before was finally resolved in the validation stage.

BEFORE

6. Xander invested P35,000.00 in a savings account that pays 4% simple interest. How much will he earn after 3 years? What will the new balance be?

$P = 35,000$
 $r = 4\% \text{ or } 0.04$
 $t = 3 \text{ yrs}$

$I = Prt$
 $= (35,000)(0.04)(3)$
 $= 4,200$
 $35,000 + 4,200 = 39,200$

AFTER

6. Xander invested P35,000.00 in a savings account that pays 4% simple interest. How much will he earn after 3 years? What will the new balance be?

Known:
 ① → money of Xander which is P35,000
 → interest is 4% = 0.04
 → 3 years
 Type: Money Relations

Unknown:
 → How much will he earn in 3 years?
 → What will be the new balance?

② Let $x = \text{interest}$
 $y = \text{be the annual balance w/ 4\% interest}$

$(35,000 \times 0.04) 3 = x$

Therefore, he will earn 4,200 for 3 years
 → His new balance is P39,200

$$\begin{array}{r}
 \text{P } 35,000 \\
 \times \quad .04 \\
 \hline
 \text{P } 1,400 \\
 \text{1st year} \leftarrow \\
 \hline
 \text{P } 36,400 \\
 + \text{P } 1,400 \\
 \hline
 \text{2nd year} \leftarrow \text{P } 37,800 \\
 + \text{P } 1,400 \\
 \hline
 \text{3rd year} \leftarrow \text{P } 39,200
 \end{array}$$

Figure 21: Pre-Post Solution of Male #2

Difficulty/ies: LB; Coping Strategy: DP8

The student struggled in the looking-back (LB) phase (Figure 22). After utilizing the strategy of looking for more exercises and reading more books with related problems (DP8), the student was able to check with the correct computation and with a concluding statement. Generally, the student's difficulty, which is looking back before, was totally resolved after the validation stage.

BEFORE

1. Dewye is twice as old as Jean. Three years ago, the sum of their ages is 39.
How old are they?

1. Known: Dewye is twice as old as Jean
- 3 years ago, the sum of their age is 39.
Unknown: How old are they

2. $2x = \text{Dewye}$
 $x = \text{Jean}$
 $39 = \text{sum of their age}$

3. $x = 13$
 $(2x + 3) + (x + 3) = 39$
 $4(13) + 6 = 39$

4. $x = 13$ 3 years ago = 39
 $4. (2(13) + 3) + (13 + 3) =$
 $(26 + 3) + (16) =$
 $29 + 16 =$
Jean = 16 Dewye = 32

AFTER

Known: Dewye is twice as old as Jean
Unknown: age of each

Let $x = \text{age of Jean}$ $x - 3$
 $2x = \text{age of Dewye}$ $2x - 3$

$(x - 3) + (2x - 3) = 39$
 $3x - 6 = 39$
 $3x = 45$
 $x = 15$ Jean
 $2x = 30$ Dewye

3 years ago
 $15 - 3 = 12$
 $30 - 3 = 27$
 39

Therefore, Dewye is 30 yo, and Jean is 15yo

Figure 22: Pre-Post Solution of Male #5

Difficulty: LB; Coping Strategy: DP8

A summary of the pre-post test results of the validation samples (males) is presented in Table 10, showing a reduction or a total eradication of the frequency of pre-identified difficulties.

Table 10: Model validation of coping strategies of male students by phase

MALE #	Coping Strategies				Difficulty	
	Understanding the Problem (UP)	Devising a Plan (DP)	Carrying out the Plan (CP)	Looking Back (LB)	Before	After
1	UP2	DP7	CP8	LB1	DP, CP, LB	LB
2	UP8	DP8	CP4	LB2	LB	-
3	UP3	DP8	CP7	LB10	LB	-
4	UP5	DP8	CP7	LB4	CP	-
5		DP8			LB	-
6	UP8	DP8	CP1	LB3	DP, CP, LB	CP, LB
7	UP1	DP1	CP7	LB1	LB	-
8	UP2	DP8	CP2	LB1	CP, LB	LB

Looking at the solution (Figure 23), the student failed in forming the mathematical equation (DP). She knew how to operate the equation she had formed, so that she even had a concluding statement. However, after seeking assistance from friends/teacher/tutor, she was able to form the correct mathematical equation. With this, her difficulties of devising a plan were resolved.

BEFORE

10. If the digits of a two-digit number are reversed, the number is increased by 36. The sum of the digits in the number is three times their difference. What is the number? (Feliciano and Uy, 1991)

Handwritten work:

$x = \text{Tens}$
 $y = \text{Ones}$
 $10y + x = 10x + y + 36$
 $9y - 9x = 36$
 $y - x = 4$ (A)

$x + y = 3(x - y)$
 $x + y = 3x - 3y$
 $2x - 4y = 0$
 $x - 2y = 0$ (B)

Substitution method:
 Substitute value of $y \rightarrow$ (A)
 $-9 \cdot x = 4$
 $-x = \frac{4}{9}$
 $x = -\frac{4}{9}$
 Therefore, the answer is -84

Elimination method:
 Add (A) & (B)
 $-x + y = 4$
 $x - 2y = 0$
 $\hline -y = 4$
 $y = -4$

After

Let $x = \text{Tens}$
 $y = \text{Ones}$

$10x + y = 10y + x + 36$
 $9x - 9y = 36$
 $x - y = 4$

$x + y = 3(x - y)$
 $x + y = 3x - 3y$
 $-2x + 4y = 0$
 $-x + 2y = 0$

$x - y = 4$
 $-x + 2y = 0$
 $\hline y = 4$

Substituting for x: $x - y = 4$
 $x - 4 = 4$
 $x = 8$

Therefore, the number is 84

Figure 23: Pre-Post Solution of Female #2;
 Difficulty: DP; Coping Strategy: CP7

This student (Figure 24) was able to perform only the first phase of the problem-solving. Then, after utilizing the strategies of looking for more exercises and reading more books with related problems (DP8), and by seeking assistance from friends/teacher/tutor (CP7), she was able to perform all the phases of the problem-solving. Hence, her difficulties were totally resolved.

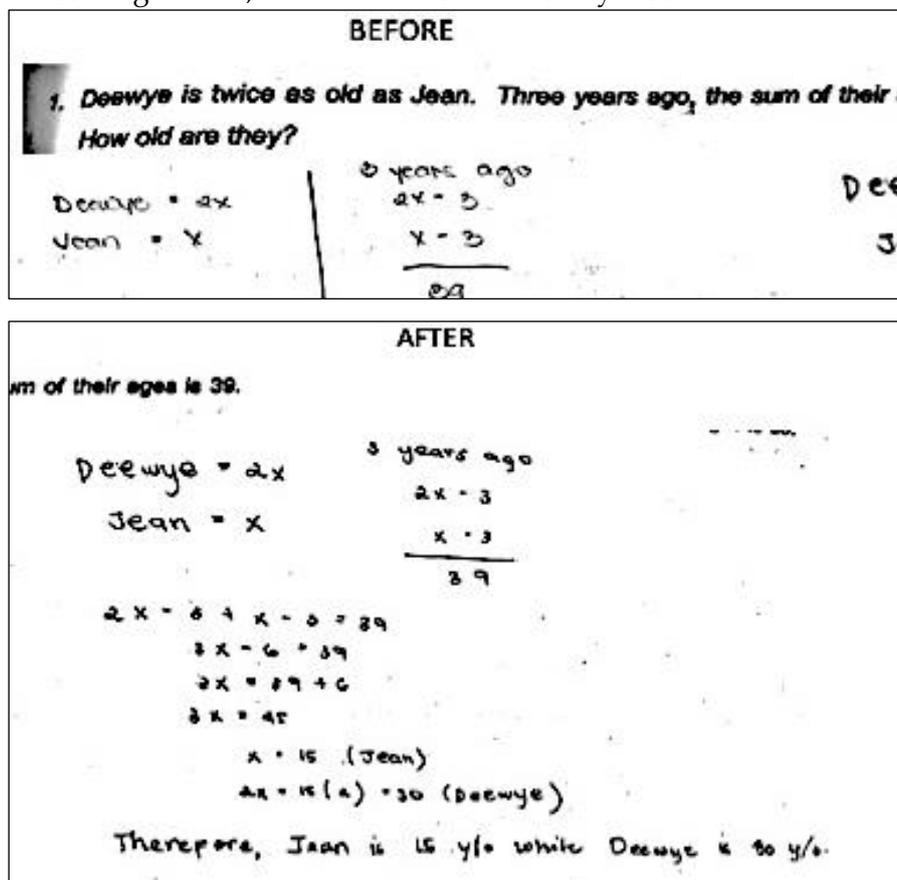


Figure 24: Pre-Post Solution of Female #4; Difficulty/ies: DP, CP, LB
Coping Strategy/ies: DP8, CP7

A summary of the pre-post test results of the validation samples (females) is presented in Table 1,1 showing a reduction or a total eradication of the frequency of pre-identified difficulties.

Table 11: Model validation of coping strategies of female students by phase

FEMALE #	Coping Strategies				Difficulty	
	Understanding the Problem (UP)	Devising a Plan (DP)	Carrying out the Plan (CP)	Looking Back (LB)	Before	After
1	UP2		CP7		DP, LB	LB
2	UP3	DP3	CP7	LB9	DP	
3	UP5	DP8	CP7	LB9	DP	-
4	UP8	DP8	CP7	LB3	DP, CP, LB	-
5	UP2	DP4	CP2	LB1	DP, CP, LB	-
6	UP3	DP8	CP7	LB9	DP	
7	UP3	DP8	CP7	LB2	DP, CP, LB	CP, LB
8	UP5	DP6	CP7	LB3	CP	-
9	UP3	DP3	CP7	LB1	CP, LB	CP
10	UP1	DP8	CP7	LB3	LB	-

Lastly, Table 12 presents the respondents from each academic program with a reduced number of their pre-identified difficulties after the post-test.

Table 12: Model validation of coping strategies by academic program by phase

Academic Program	Coping Strategies				Difficulty		Exhibit #
	(UP)	(DP)	(CP)	(LB)	Before	After	
STEM-related							
BS-ABE	UP2	DP8	CP7	LB1			
BS-ABE-B6	UP2	DP7	CP8	LB1	DP, CP, LB	LB	17 (M)
BS-ABE-A1	UP2		CP7		DP, LB	LB	25 (F)
BS-CE	UP3	DP8	CP7	LB1;LB3			
BS-CE-A13	UP5	DP6	CP7	LB3	CP	-	32 (F)
BS-CE-B16	UP3	DP3	CP7	LB1	CP, LB	CP	33 (F)
BS-CHEM E	UP2	DP5; DP8	CP1; CP7	LB1			
BS-CHEM-15	UP1	DP1	CP7	LB1	LB	-	23 (M)
BS-CHEM-4	UP5	DP5	CP6	LB8	LB		35 (F)
BS-MATH	UP3	DP8	CP7	LB1; LB2; LB3			
BS-MATH-18	UP2	DP4	CP2	LB1	DP, CP, LB	-	29 (F)
BS-MATH-4	UP3	DP8	CP7	LB9	DP	-	30 (F)
BS-MATH-22		DP8			LB	-	21 (M)
BS-METEO	UP2;UP8	DP7	CP1; CP2	LB7			
BS-METEO-3	UP8	DP8	CP4	LB2	LB		18 (M)
BS-N	UP2	DP8	CP7	LB3			
BSN-A30	UP1	DP8	CP7	LB3	LB	-	34 (F)
BSN-A33	UP2	DP8	CP2	LB1	CP, LB	-	24 (M)
BSN-A36	UP7	DP7	CP7	LB4	LB		37 (M)
NON-STEM-related							
BA-COMM	UP2	DP4	CP1; CP7	LB1; LB3			
BA-COMM-2	UP5	DP8	CP7	LB4	CP	-	20 (M)
BA-COMM-17	UP8	DP8	CP7	LB3	DP, CP, LB	-	28 (F)
BA-COMM-4	UP2	DP1	CP2	LB1	DP		36 (F)
BS-ECON	UP2	DP8	CP7	LB7			
BS-ECON-22	UP3	DP8	CP7	LB2	DP, CP, LB	-	31 (F)
BS-ECON-36	UP8	DP8	CP1	LB3	DP, CP, LB	CP, LB	22 (M)
BS-SOCIO	UP2	DP8	CP7	LB1			
BS-SOCIO-21	UP3	DP3	CP7	LB9	DP	-	26 (F)
BS-SOCIO-14	UP3	DP8	CP7	LB10	LB	-	19 (M)

5. Discussion

The models are compact descriptions of a system structure; and they can provide a derivation of the specific predictions from theory that can be tested with the data (Turchin, et al., n. d.). They have the ability to demonstrate understanding through different representations. Depending on the purpose, one can develop different models for the same empirical system. Mehta (2019) explained that model-building or mathematical-modelling uses mathematics to represent, analyze, and make predictions of real-world phenomena.

The analytical stage commenced with the administration of a problem-solving test and a coping-strategy questionnaire from 297 respondents. The results revealed two difficulties in each of the phases of problem-solving, and each respondent encountered at least one of these difficulties in all the phases. Both males and females experienced the same difficulty in all the phases, namely an inability to distinguish the known from the unknown information (U1), which shows partial similarity with the results of Pearce et al. (2013); that is the inability to transform a problem into a mathematical equation (D1), which validates the results of Dela Cruz and Lapinid (2018); as well as the inability to completely perform the working procedure systematically and accurately (C1), which supports the findings of Finney, (n.d.) and Siniguian (2017), and also an inability to start the evaluation of the correctness of the obtained solution (L2), as revealed by Siniguian (2017). The majority of the respondents of the STEM-related academic programs likewise experienced difficulties with U2, D1, C1 and L2; while the majority of the students in the non-STEM related academic programs experienced difficulties in U1, D1, C1 and L2. On the other hand, commonly utilized coping strategies are problem-focused strategies, which reinforces the findings of Carver et al., (1999); Folkman & Lazarus, 1980, Ghan, (2011); Ader & Erktin, (2012); Lazarus (1993).

The coping strategies that were elicited reveal that both sexes utilized the same coping strategies in the first three phases of the problem-solving, namely, UP2, DP8 and CP7, respectively. For the looking-back phase, the males preferred to use LB3, an emotion-focused coping strategy, which contradicts the results of Rapson (1990) and Eschenbeck et al. (2002), and LB1 for the females, which is in conflict with the findings of Brougham et al. (2009); Hammermeister & Burton (2004) and Kaiseler et al. (2012).

In addition, both groups (STEM-related and non-STEM related academic programs) adopted the same set of coping strategies in the different phases, namely, UP2, DP8, CP7 and LB1. Additionally, two coping strategies in the looking-back phase were added, which are LB3 and LB7. The students' responses were triangulated by informal conversation with unstructured interview questions to a selected number of students, and to a few teachers, who handled the identified respondents.

From the identified relationships between and among the variables, two models were developed, namely; Coping Strategy by Sex by Phase Model and Coping Strategy by Academic Program (non STEM-related and Stem-related) by Phase Model. The effectivity of the models was consequently validated through the

validation group that comprised 188 respondents. Purposive sampling, where factors like the availability of the respondents, together with their coping strategies that matched those presented in the models developed, were taken into account. From the eight male respondents, three showed a decrease in the frequency of pre-identified difficulty/ies; while five of them totally surpassed all their difficulties. For the 10 sampled female respondents, however, three showed a decrease in the frequency of pre-identified difficulty/ies; while seven of them totally surpassed their difficulties. This information concluded that the models have the ability to address the difficulties of the students in their problem-solving encounters through their coping strategies.

6. Conclusion

This study examined the students' difficulties in Mathematical problem-solving and the coping strategies that they applied in response to these difficulties. Although a number of studies have already been implemented to investigate these research variables, this study introduces a different approach of analyzing these, by relating them to factors like students' sexual orientation and academic programs. After the data analysis, the developed models were found to help address the students' difficulties. They were able to either reduce, or totally eradicate the frequency of the students' pre-identified Mathematical problem-solving difficulties. Such findings would input a novel contribution to the literature on educational assessment, specifically in Mathematical problem-solving, since literature and studies dealing with this area are scarce. This study recommends that future research should focus on the extensive identification of the problem-solving difficulties in each of Polya's (1945) problem-solving phases.

A larger scope on the population may be considered. The focus may not only be on the secondary or tertiary education students, rather, the pre-schoolers and the elementary pupils, could be included. The studies show that an interest in numbers and numerical phenomena starts at an early age, like the preschool, or the kindergarten. In their young minds, they should become aware of the fundamental numeric skills and other cognitive foundations that are relevant in learning through mathematics education. Through it, difficulties in problem-solving may be reduced and perhaps may become non-existent as they step up in the educational ladder. Scope in terms of locale may also be considered like provincial or regional with varied dependent variables. Furthermore, future research projects may be conducted on a long-term basis to investigate whether there would be an improvement in the Mathematics problem-solving performance of the students, as their teachers employ the recommended coping strategies presented in the models.

In addition, during this time of pandemic, educators should explore students' problem-solving difficulties and their coping mechanisms in online learning.

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